CAMBRIDGE
International Education

Cambridge International AS & A Level

MATHEMATICS **9709/12**

Paper 1 Pure Mathematics 1 **February/March 2025**

MARK SCHEME

Maximum Mark: 75

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the February/March 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:
Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:
Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:
Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics Specific Marking Principles

1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.

6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

Annotations guidance for centres

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

Annotations

Annotation	Meaning
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Independent accuracy mark awarded zero
	Independent accuracy mark awarded one
	Independent accuracy mark awarded two
	Benefit of the doubt
	Blank Page
	Incorrect point

Annotation	Meaning
Dep	Used to indicate DM0 or DM1
DM1	Dependent on the previous M1 mark(s)
FT	Follow through
~~	Indicate working that is right or wrong
Highlighter	Highlight a key point in the working
ISW	Ignore subsequent work
J	Judgement
JU	Judgement
M0	Method mark awarded zero
M1	Method mark awarded one
M2	Method mark awarded two
MR	Misread
O	Omission or Other solution
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
PE	Judgment made by the PE

Annotation	Meaning
Pre	Premature approximation
SC	Special case
SEEN	Indicates that work/page has been seen
SF	Error in number of significant figures
✓	Correct point
TE	Transcription error
XP	Correct answer from incorrect working

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

DM or **DB** When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

Question	Answer	Marks	Guidance
1	$[kx+13=5+3x-2x^2 \Rightarrow]\ 2x^2+(k-3)x+8\ [=0]$	**B1**	OE Eliminate y to obtain a three-term quadratic.
	Use of $b^2-4ac<0$ or $b^2-4ac=0$ with *their* coefficients of *their* new quadratic equation. Condone ± errors only.	**M1**	OE Use of '>0' scores M0, unless recovered.
	–5 and 11	**A1**	Identification of correct critical values, may only be seen in their final answer.
	$-5<k<11$	**A1**	CWO Do not allow 'or'. A0 if $\leqslant$ sign or signs used.
		4	

Question	Answer	Marks	Guidance
2(a)	$4x+\frac{5}{x^2}$	**B1**	OE
	$\left[\frac{dy}{dx}=\right]\ 9$	**B1 FT**	Correct use of $x=1$ in *their* two-term differentiated expression, defined as an expression with one correct power.
		2	

Question	Answer	Marks	Guidance
2(b)	*Their* $\left(4x+\frac{5}{x^2}\right)=0$ and valid method as far as '$x=...$'	**M1**	Equate their derivative of the form $Ax\pm\frac{B}{x^2}$ to zero, where $A,\ B\neq 0$, and solve. If no working is seen, this can be implied by a correct answer for x.
	$x=-1.08$	**A1**	AWRT
	$y=9.96$	**A1**	AWRT
		3	

Question	Answer	Marks	Guidance
3(a)	$(2x)^4$ and $\left(\frac{\pm 3}{x}\right)^4$	**B1**	May be seen in a full expansion. This can be implied by $16x^4$ and $+\frac{81}{x^4}$ unless they are clearly using $+\frac{3}{x}$ throughout.
	$4(2x)^3\left(\frac{-3}{x}\right)+6(2x)^2\left(\frac{-3}{x}\right)^2+4(2x)\left(\frac{-3}{x}\right)^3$	**B1**	Correct combination of numerical coefficients for the middle three terms. Can be implied by a correct full expansion.
	$\left[16x^4\right]+k_1x^2+k_2\left[x^0\right]+k_3x^{-2}\left[+81x^{-4}\right]$	**M1**	OE Powers now simplified correctly with *their* $k_1,\ k_2,\ k_3\neq 0$.
	$16x^4-96x^2+216-216x^{-2}+81x^{-4}$	**A1**	OE
		4	

Question	Answer	Marks	Guidance
3(b)	Use of (*their* 216) + 5×(*their* –96) only, to arrive at the coefficient of x^2	**M1**	Other terms may be seen.
	–264	**A1**	Accept $-264x^2$ as the final answer.
		2	

Question	Answer	Marks	Guidance
4(a)	6×0.8	**B1**	Accept $\frac{45.8}{360}\times12\pi$.
	$AB^2 = 10^2+10^2-2\times10\times10\cos0.8$ or $AB = 2(10\sin0.4)$ or $AB = \frac{10\sin0.8}{\sin\left(\frac{\pi-0.8}{2}\right)}$	**M1**	Allow angles correctly converted to degrees for this mark. $0.8\,\text{rad} = 45.8°$, $O\hat{A}B = O\hat{B}A = 67.1°$. $\left(\frac{\pi-0.8}{2}\right) = 1.17$ This mark can be implied by AWRT 7.8.
	20.6	**A1**	AWRT
		3	
4(b)	[Area of sector =] $\frac{1}{2}\times6^2\times0.8$	**B1**	
	[Area of triangle =] $\frac{1}{2}\times10^2\times\sin0.8$ or $10\sin0.4\times10\cos0.4$ or other complete method.	**M1**	OE Allow use of *their* value of θ or $\frac{1}{2}\theta$ in degrees.
	21.5	**A1**	AWRT
		3	

Question	Answer	Marks	Guidance
5	Attempt to solve either: $5+(n-1)6=150$ or $5+(n-1)6=400$	**M1**	Attempt to determine positions of first and last terms involved
	$\frac{151}{6}$ and $\frac{401}{6}$	**A1**	OE Can be implied by 25 or 26 and 66 or 67.
	Correct use of S_n formula with *their* 66 and *their* 25	**M1**	
	$S_{66\,or\,67}-S_{25\,or\,26}$	**M1**	
	$S_{66}-S_{25}$	**A1**	
	11275	**A1**	
	Alternative Method for Question 5:		
	Attempt to find new *a* and *l* for reduced series	**M1**	
	155 and 395	**A1**	
	$their\,395=their\,155+(n-1)6$	**M1**	Attempt to find *n*, which results in 40, 41 or 42.
	$n=41$	**A1**	CWO
	$S_{their\,41}=\frac{their\,41}{2}(their\,155+their\,395)$	**M1**	OE
	11275	**A1**	
		6	

Question	Answer	Marks	Guidance
6(a)	$(r+5,\ r+8)$	**B1**	OE Allow $x=r+5,\ y=r+8$. If values are stated without reference to x and y, take the first value to be *their* x.
		1	
6(b)	$\textit{their}(r+5)^2+\textit{their}(r+8)^2=15^2$	**B1 FT**	OE Following *their* answers to **(a)**, which must both contain r.
	$\left[r^2+13r-68[=0]\Rightarrow\right]\ (r+17)(r-4)[=0]$	**M1**	Or other valid method of solution for *their* three-term quadratic.
	$[r=]4$	**A1**	CWO $r=-4\Rightarrow r=4$ scores A0.
			Special Case: After B1M0, $r=4$ scores **SCB1**, but after B1M0, $r=-4\Rightarrow r=4$ scores B0.
		3	
6(c)	$\dfrac{\textit{their}(r+8)}{\textit{their}(r+5)}$ from **(a)** with *their* r from **(b),** or $\dfrac{(\textit{their}\ r\ \text{from}(\mathbf{b}))+8}{(\textit{their}\ r\ \text{from}(\mathbf{b}))+5}$	**M1**	$r>0$ only.
	$-\dfrac{3}{4}$	**A1 FT**	OE, i.e. $-\dfrac{\textit{their}(r+5)}{\textit{their}(r+8)}$ or $-\dfrac{(\textit{their}\ r\ \text{from}(\mathbf{b}))+8}{(\textit{their}\ r\ \text{from}(\mathbf{b}))+5}$.
		2	

Question	Answer	Marks	Guidance
7(a)	Use of $\tan^2\theta = \dfrac{\sin^2\theta}{\cos^2\theta}$	**M1**	
	Relevant use of $\cos^2\theta = 1-\sin^2\theta$ at least once	**M1**	
	$\dfrac{8\sin^2\theta - 5\sin^4\theta}{1-\sin^2\theta}$	**A1**	**AG** All necessary detail needed.
		3	
7(b)	Attempt to solve *their* $5\sin^4\theta - 17\sin^2\theta + 9 = 0$ using a "correct" method	***M1**	Allow ± errors in arriving at *their* quadratic in $\sin^2\theta$. This can be implied by either $\left[\sin^2\theta =\right]$ 2.744 or 0.6559.
	$\sin\theta = [\pm]0.81[0]$ or $\sqrt{\dfrac{17-\sqrt{109}}{10}}$	**A1**	Condone inclusion of $\sin\theta = 1.65$ for this mark. Allow $\sqrt{\dfrac{17\pm\sqrt{109}}{10}}$. This mark can be implied by correct values.
	Their 54.1, and $180 - $ *their* 54.1 or $180 + $ *their* 54.1	**DM1**	A correct method for obtaining a second angle within the range $0 <$ *their* $54.1 < 90$.
	54.1, 125.9, 234.1	**A1**	AWRT A0 for additional values between $0°$ and $270°$.
		4	

Question	Answer	Marks	Guidance
8(a)	$ar=-120$ and $\frac{a}{1-r}=160$	**B1**	
	$-\frac{120}{r}\times\frac{1}{1-r}=160$ or $\frac{a}{1+\frac{120}{a}}=160$	**M1**	Elimination of either a or r. Condone ± errors for this mark.
	$4r^2-4r-3[=0]$ or $a^2-160a-19200[=0]$	**A1**	OE Rearrange to arrive at a three-term quadratic.
	$r=-\frac{1}{2}$ only	**A1**	
		4	

Question	Answer	Marks	Guidance
8(b)	[$a =$] 240	**B1 FT**	$-120 \div (their\ r)$, where $-1 < r < 1$, $r \neq 0$.
	$160 - \dfrac{240\left(1-(-\frac{1}{2})^9\right)}{1-\left(-\frac{1}{2}\right)}$	**M1**	With (*their* 240) and $(their\ r)$ as long as $-1 < r < 1$, $r \neq 0$. Condone reversed subtraction.
	Alternative Method 1 for first two marks of Question 8(b)		
	[$a =$] 240	**B1 FT**	$-120 \div (their\ r)$, where $-1 < r < 1$, $r \neq 0$.
	$\dfrac{240 \times (-\frac{1}{2})^9}{1-\left(-\frac{1}{2}\right)}$	**M1**	Correctly using the 10th term as 'a' and the sum to infinity. With (*their* 240) and $(their\ r)$ as long as $-1 < r < 1$, $r \neq 0$.
	Alternative Method 2 for first two marks of Question 8(b)		
	[10th term =] $-\frac{15}{32}$, 0.46875 OE	**B1 FT**	$-120 \div (their\ r)^8$, where $-1 < r < 1$, $r \neq 0$.
	$\dfrac{-\frac{15}{32}}{1-\left(-\frac{1}{2}\right)}$	**M1**	With $(their\ a \text{ and } r)$, where $-1 < r < 1$, $r \neq 0$.
	$-\frac{5}{16}$ or -0.3125	**A1**	A0 for –0.313 without sight of $-\frac{5}{16}$ or –0.3125. Condone use of $r = \frac{3}{2}$ to provide a second solution.
		3	

Question	Answer	Marks	Guidance
9(a)	$\frac{6}{\left(\frac{1}{2}\right)^4} - \frac{5}{\left(\frac{1}{2}\right)^3}$	**M1**	Substitute $x = \frac{1}{2}$ and evaluate second derivative.
	$96 - 40[= 56] > 0 \Rightarrow$ Minimum	**A1**	CWO Evidence and conclusion. **SC B1** for $\frac{\mathrm{d}^2y}{\mathrm{d}x^2} > 0$ without sight of $96 - 40$ or 56.
		2	

Question	Answer	Marks	Guidance
9(b)	$\left\{\frac{6}{-3}x^{-3}\right\}\left\{-\frac{5}{-2}x^{-2}\right\}[+c_1]$	**B1 B1**	OE B1 for each correct { }.
	$0=\frac{6}{-3}\left(\frac{1}{2}\right)^{-3}-\frac{5}{-2}\left(\frac{1}{2}\right)^{-2}+c_1$	**M1**	Substitute $x=\frac{1}{2}$ into two terms of an integrated expression (at least one correct power), now with c_1, and equate to 0 to find c_1.
	$c_1=6$	**A1**	
	$k_1x^{-2}+k_2x^{-1}+k_3x\ \ [+c_2]$	**M1**	Integration of *their* $\frac{\mathrm{d}y}{\mathrm{d}x}$ to produce at least two terms with correct powers, $k_1, k_2 \neq 0$.
	$9=\frac{1}{\left(\frac{1}{2}\right)^2}-\frac{5}{2\left(\frac{1}{2}\right)}+6\left(\frac{1}{2}\right)+c_2$	**M1**	OE Substitute $\left(\frac{1}{2}, 9\right)$ into integrated expression (at least two correct powers) to find c_2.
	$y=x^{-2}-\frac{5}{2}x^{-1}+6x+7$	**A1**	OE Condone their final answer being $c_2=7$ if a completely correct simplified expression for the equation containing c_2 has been stated previously.
		7	

Question	Answer	Marks	Guidance
10(a)	$\left\{\frac{2}{3}\times\frac{4}{3}(3x+4)^{\frac{3}{2}}\right\}\left\{-\frac{2x^2}{2}-6x\right\}$	**B1 B1**	B1 for each correct { }.
	$[A=]\left(\frac{8}{9}(21+4)^{\frac{3}{2}}-7^2-6\times7\right)-\left(\frac{8}{9}(4)^{\frac{3}{2}}\right)$	**M1**	Correct use of 7 and 0 in an expression with at least two terms with two correct powers.
	13	**A1**	
		4	

Question	Answer	Marks	Guidance
10(b)	$\left(2(3x+4)^{-\frac{1}{2}}\times 3\right)-2$	**B1**	
	$y-0=\left(their\ \frac{\mathrm{d}y}{\mathrm{d}x}\ with\ x=7\right)(x-7)$	***M1**	Using $x=7$, *their* value for $\frac{\mathrm{d}y}{\mathrm{d}x}$ and then any form of the equation of a straight line using $(7, 0)$.
	Either:		
	[Q is] $\left(0, \frac{28}{5}\right)$	**DM1**	Use $x=0$ in *their* equation of PQ.
	[Area of OPQ =] $\frac{1}{2}\times 7\times\left(their\ \frac{28}{5}\right)$	**DM1**	
	$\left[\frac{1}{2}\times 7\times\left(their\ \frac{28}{5}\right)-\left(their\ 13\ \text{from}\left(\mathbf{a}\right)\right)\right]=\frac{33}{5}$	**A1 FT**	Only FT, following B0M1DM1DM1, from *their* **(a)** if $\left(their\ 13\ \text{from}\left(\mathbf{a}\right)\right)<\frac{98}{5}$ and the area is > 0.
	Or:		
	$\int\left(their\left(-\frac{4}{5}(x-7)\right)\right)\mathrm{d}x$	**DM1**	
	Evaluating $their\left(-\frac{4}{5}\left(\frac{x^2}{2}-7x\right)\right)$ with limits 7 and 0	**DM1**	

Question	Answer	Marks	Guidance
10(b)	$\left[\left(their\ \text{area of } OPQ\right)-\left(their 13\ from\left(\boldsymbol{a}\right)\right)\right]=\frac{33}{5}$	**A1 FT**	Only FT, following B0M1DM1DM1, from their **(a)** if $\left(their 13\ from\left(a\right)\right)<\frac{98}{5}$ and the area is > 0.
		5	

Question	Answer	Marks	Guidance
11(a)	State or imply $g^{-1}\left(x\right)=\frac{1}{2}\left(x-k\right)$ or equivalent	**B1**	
	Obtain $\frac{1}{2}\left(3k+1-k\right)=c$ and hence $2k+1=2c$	**B1**	OE
	Or:		
	$g\left(c\right)=3k+1$	**B1**	
	$[\ 2c+k=3k+1\Rightarrow]\ 2c=2k+1$	**B1**	OE
	Then:		
	$\left[gf\left(x\right)=\right]\ 2\left(4x^2-c\right)+k$	**M1**	Allow ± errors only.
	$\left[8x^2-2c+k\Rightarrow 8x^2-\left(2k+1\right)+k\Rightarrow\right]\ gf\left(x\right)=8x^2-k-1$	**A1**	**AG** All necessary detail needed.
		4	

Question	Answer	Marks	Guidance
11(b)	$8(x-2)^2-k-1+3$	**B1**	OE Translation coming before the stretch
	$k\left(their\left(8(x-2)^2-k-1+3\right)\right)$	**B1 FT**	OE Stretch
	$\left[h(x)=\right]-\left(k\left(their\left(8(x-2)^2-k-1+3\right)\right)\right)$	**B1 FT**	OE Reflection
		3	
11(c)	$k^2-2k=15$ or $k^2-2k\leqslant 15$	**B1**	OE
	$k=5$ only	**B1**	
	$c=\frac{11}{2}$ only	**B1**	OE
		3	